

IG - Maths  
0580

Matrices

Exercise - Paper 2.

Q1 Workout. (a)  $\begin{pmatrix} 2 & 1 \\ 4 & 3 \end{pmatrix}^2$  --- [2]

(b)  $\begin{pmatrix} 2 & 1 \\ 4 & 3 \end{pmatrix}^{-1}$  --- [2]

SP-15/02/Q11

Q2  $M = \begin{pmatrix} 5 & 3 \\ 1 & -2 \end{pmatrix}$   $N = \begin{pmatrix} 3 & -6 \\ 4 & 2 \end{pmatrix}$

Calculate: (a)  $MN$  --- [2]

(b)  $M^{-1}$  --- [2]

Q3

$M = \begin{pmatrix} -2 & 0 \\ 5 & -6 \end{pmatrix}$   $N = \begin{pmatrix} -3 & 1 \\ 0 & -1 \end{pmatrix}$

M-17/22/Q18

W-17/23/Q19

(a) Work out  $NM$  --- [2]

(b) Find  $M^{-1}$ , the inverse of  $M$ . --- [2]

Q4 Find the inverse of the matrix  $\begin{pmatrix} 3 & -2 \\ -8 & 7 \end{pmatrix}$  --- [2]

M-16/22/Q8

Q5  $M = \begin{pmatrix} 5 & 1 \\ -3 & -2 \end{pmatrix}$

S-16/22/Q22

(a) Work out  $4M$  --- [2]

(b) Work out  $M^2$  --- [2]

(c) Find  $M^{-1}$ , the inverse of  $M$ . --- [2]

Q6 Workout. (a)  $2 \begin{pmatrix} 3 \\ 5 \end{pmatrix} - \begin{pmatrix} 1 \\ 2 \end{pmatrix}$  --- [1]

W-16/21/Q15

(b)  $\begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix}$  --- [2]

Q7 (a) Find the inverse of  $\begin{pmatrix} 2 & -3 \\ 5 & -4 \end{pmatrix}$  --- [2]

(b) The matrix  $\begin{pmatrix} w & -9 \\ 4 & w-12 \end{pmatrix}$  does not have an inverse.

Find the value of  $w$ .

--- [4]

W-16/22/Q19

Q8  $A = \begin{pmatrix} 4 & 2 \\ 2 & 1 \end{pmatrix}$   $B = \begin{pmatrix} 7 & -3 \\ 4 & 5 \end{pmatrix}$   $C = \begin{pmatrix} -2 & 3 & 1 \\ 4 & 5 & -1 \end{pmatrix}$   $D = \begin{pmatrix} -9 \\ 0 \end{pmatrix}$

(a) Which of these four matrix calculations is not possible.

$A+B$  :  $3C$   $CB$   $AD$  --- [1]

(b) Calculate  $AB$  --- [2]

(c) Work out  $B^{-1}$ , the inverse of  $B$ . --- [2]

(d) Explain why  $A$  does not have an inverse. --- [1]

W-16/23/Q25

Q9  $A = \begin{pmatrix} 8 & 3 \\ 4 & 2 \end{pmatrix}$  find: (a)  $A^2$  --- [2]  
(b)  $A^{-1}$  M-15/22/Q15 --- [2]

Q10 (a) Calculate  $\begin{pmatrix} 3 & 7 \\ -1 & 4 \end{pmatrix} \begin{pmatrix} -2 & 1 \\ 4 & 2 \end{pmatrix}$  S-15/21/Q22 --- [2]

(b) Calculate the inverse of  $\begin{pmatrix} 5 & 3 \\ 6 & 4 \end{pmatrix}$  --- [2]

Q11  $M = \begin{pmatrix} 3 & 1 \\ -11 & -2 \end{pmatrix}$

Find  $M^{-1}$ ; the inverse of  $M$ . S-15/22/Q11 --- [2]

Q12 (a) Work out  $\begin{pmatrix} 1 & -2 \\ 3 & 4 \end{pmatrix} \begin{pmatrix} -5 & -3 \\ 2 & 1 \end{pmatrix}$  --- [2]

(b) Find the inverse of  $\begin{pmatrix} 1 & -2 \\ 3 & 4 \end{pmatrix}$  --- [2]

(c) Explain why it is not possible to work out  $\begin{pmatrix} 1 & -2 \\ 3 & 4 \end{pmatrix} + \begin{pmatrix} 3 \\ 2 \end{pmatrix}$  --- [1]

Q13  $M = \begin{pmatrix} 3 & -4 \\ -2 & 4 \end{pmatrix}$   $N = \begin{pmatrix} 5 & 0 \\ 1 & 2 \end{pmatrix}$  W-15/22/Q7 --- [2]  
Calculate  $MN$ .

Q14  $M = \begin{pmatrix} 7 & u \\ 2 & 3 \end{pmatrix}$  and  $|M| = 1$

Find the value of  $u$ .

W-15/23/Q13

--- [2]

Q15  $A = \begin{pmatrix} 2 & 8 \\ 1 & 4 \end{pmatrix}$  work out  $A^2 - 4A$ . --- [3]  
W-14/21/Q14

Q16  $A = \begin{pmatrix} 3 & -2 \\ 1 & 4 \end{pmatrix}$   $B = \begin{pmatrix} 2 & 0 \\ -5 & 7 \end{pmatrix}$   
 (a) Calculate  $BA$ . --- [2]  
 (b) Find the determinant of  $A$ . --- [1]  
W-14/22/Q11

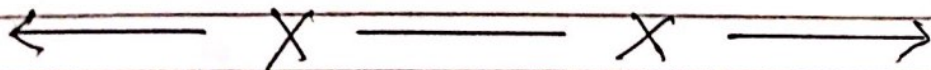
Q17  $M = \begin{pmatrix} 4 & 2 \\ 3 & 5 \end{pmatrix}$  Find (a)  $M^2$  --- [2]  
 (b) the determinant of  $M$ . --- [1]  
S-14/22/Q15

Q18  $A = \begin{pmatrix} 5 & 2 \\ 4 & 3 \end{pmatrix}$  (a) Calculate  $A^2$  --- [2]  
 (b) Calculate  $A^{-1}$ . --- [2]  
S-14/23/Q18

Q19  $A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$   $B = \begin{pmatrix} 4 & 3 \\ 1 & 2 \end{pmatrix}$   
 Find.  
 (a)  $AB$  --- [2]  
 (b)  $B^{-1}$  --- [2]  
S-13/21/Q24

Q20  $M = \begin{pmatrix} 2 & 3 \\ 3 & 6 \end{pmatrix}$   $N = \begin{pmatrix} 2 & 1 & 5 \\ 1 & 7 & 2 \end{pmatrix}$   
 (a) Work out  $MN$  --- [2]  
 (b) Find  $M^{-1}$  --- [2]  
S-13/23/Q17

Q21  $A = \begin{pmatrix} 3 & -1 \\ 4 & 2 \end{pmatrix}$   $I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$   
 work out the following.  
 (a)  $AI$  [1]  
 (b)  $A^{-1}$  [2]  
W-13/23/Q11



Answers

Q1 (a)  $\begin{pmatrix} 8 & 5 \\ 20 & 13 \end{pmatrix}$  (b)  $\begin{pmatrix} 1\frac{1}{2} & -\frac{1}{2} \\ -2 & 1 \end{pmatrix}$  Q13  $\begin{pmatrix} 11 & -8 \\ -6 & 8 \end{pmatrix}$

Q2 (a)  $\begin{pmatrix} 27 & -24 \\ -5 & -10 \end{pmatrix}$  (b)  $-\frac{1}{13} \begin{pmatrix} -2 & -3 \\ -1 & 5 \end{pmatrix}$

Q14 6  
Q15  $\begin{pmatrix} 4 & 16 \\ 2 & 8 \end{pmatrix}$

Q3 (a)  $\begin{pmatrix} 11 & -6 \\ -5 & 6 \end{pmatrix}$  (b)  $\frac{1}{12} \begin{pmatrix} -6 & 0 \\ -5 & -2 \end{pmatrix}$

Q16 (a)  $\begin{pmatrix} 6 & -4 \\ -8 & 38 \end{pmatrix}$  (b) 14

Q4  $\frac{1}{5} \begin{pmatrix} 7 & 2 \\ 8 & 3 \end{pmatrix}$

Q18  $\begin{pmatrix} 33 & 16 \\ 32 & 17 \end{pmatrix}$  (b)  $\frac{1}{7} \begin{pmatrix} 3 & -2 \\ -4 & 5 \end{pmatrix}$

Q5 (a)  $\begin{pmatrix} 20 & 4 \\ -12 & -8 \end{pmatrix}$  (b)  $\begin{pmatrix} 22 & 3 \\ -9 & 1 \end{pmatrix}$

Q19 (a)  $\begin{pmatrix} 6 & 7 \\ 16 & 17 \end{pmatrix}$  (b)  $\frac{1}{5} \begin{pmatrix} 2 & -3 \\ -1 & 4 \end{pmatrix}$

(c)  $-\frac{1}{7} \begin{pmatrix} -2 & -1 \\ 3 & 5 \end{pmatrix}$

Q20 (a)  $\begin{pmatrix} 7 & 23 & 16 \\ 12 & 45 & 27 \end{pmatrix}$

(b)  $\frac{1}{3} \begin{pmatrix} 6 & -3 \\ -3 & 2 \end{pmatrix}$

Q6 (a)  $\begin{pmatrix} 5 \\ 8 \end{pmatrix}$  (b) (8)

Q21 (a)  $\begin{pmatrix} 3 & -1 \\ 4 & 2 \end{pmatrix}$  (b)  $\frac{1}{10} \begin{pmatrix} 2 & 1 \\ -4 & 2 \end{pmatrix}$

Q7 (a)  $\frac{1}{7} \begin{pmatrix} -4 & 3 \\ -5 & 2 \end{pmatrix}$  (b) 6

Q8 (a) CB (b)  $\begin{pmatrix} 36 & -2 \\ 18 & -1 \end{pmatrix}$

← X — X →

(c)  $\frac{1}{47} \begin{pmatrix} 5 & 3 \\ -4 & 7 \end{pmatrix}$  (d) as  $|A|=0$

Q9 (a)  $\begin{pmatrix} 76 & 30 \\ 40 & 16 \end{pmatrix}$  (b)  $\frac{1}{4} \begin{pmatrix} 2 & -3 \\ -4 & 8 \end{pmatrix}$

Q11  $\frac{1}{5} \begin{pmatrix} -2 & -1 \\ 11 & 3 \end{pmatrix}$

Q10 (a)  $\begin{pmatrix} 22 & 17 \\ 18 & 7 \end{pmatrix}$  (b)  $\frac{1}{2} \begin{pmatrix} 4 & -3 \\ -6 & 5 \end{pmatrix}$

Q12 (a)  $\begin{pmatrix} -9 & -5 \\ -7 & -5 \end{pmatrix}$  (b)  $\frac{1}{10} \begin{pmatrix} 4 & 2 \\ -3 & 1 \end{pmatrix}$

(c) Not the same order.